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Appendix J: Statistical Probability Analysis for  
Estimating Direct Strike Impact and Number of  
Potential Exposures from Military Expended  
Materials



**Supplemental Environmental Impact Statement/  
Overseas Environmental Impact Statement  
Mariana Islands Training and Testing**

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## APPENDIX J Statistical Probability Analysis for Estimating Direct Strike Impact and Number of Potential Exposures from Military Expended Materials

This Appendix discusses the methods and results for calculating the probability of the direct strike of an animal by any military items from the proposed training and testing activities falling toward (or directed at) the sea surface. For the purposes of this section, military items include non-explosive practice munitions, sonobuoys, acoustic countermeasures, some targets, torpedoes, anchors, and high-energy lasers. Only marine mammals and sea turtles will be analyzed using these methods because animal densities are necessary to complete the calculations, and density estimates are currently only available for marine mammals and sea turtles within the Study Area. The analysis conducted here does not account for explosive munitions because impacts from explosives are analyzed within the Navy Acoustic Effects Model as described in *Quantifying Acoustic Impacts on Marine Mammals and Sea Turtles: Methods and Analytical Approach for Phase III Training and Testing* (U.S. Department of the Navy, 2017).

### J.1 DIRECT IMPACT ANALYSIS

These calculations estimate the impact probability (P) and number of exposures (T) associated with direct impact of military items on marine animals on the sea surface within the training or testing area in which the activities are occurring (R = area of the Mariana Islands Range Complex). The statistical probability analysis is based on probability theory and modified Venn diagrams with rectangular “footprint” areas for the individual animal (A) and total impact (I) inscribed inside the training or testing area (R). The analysis is over-predictive and conservative, in that it assumes: (1) that all animals would be at or near the surface 100 percent of the time, when in fact, marine mammals spend the majority of their time underwater, and (2) that the animals are stationary, which does not account for any movement or potential avoidance of the training or testing activity.

1.  $A = \text{length} \times \text{width}$ , where the individual animal’s width (breadth) is assumed to be 20 percent of its length for marine mammals and 112 percent of its length for sea turtles. A is multiplied by the number of animals  $N_a$  in the training or testing area (i.e., product of the highest average seasonal animal density [D] and training or testing area [R]:  $N_a = D \times R$ ) to obtain the total animal footprint area ( $A \times N_a = A \times D \times R$ ) in the training or testing area. As a conservative scenario, the total animal footprint area is calculated for the species with the highest average seasonal density (pantropical spotted dolphins).
2.  $I = N_{\text{mun}} \times \text{length} \times \text{diameter}$ , where  $N_{\text{mun}}$  = total annual number of military items for each type, and “length” and “diameter” refer to the individual military equipment dimensions. For each type, the individual impact footprint area is multiplied by the total annual number of military items to obtain the type-specific impact footprint area ( $I = N_{\text{mun}} \times \text{length} \times \text{diameter}$ ). Each training or testing activity uses one or more different types of military items, each with a specific number and dimensions, and several training and testing events occur in a given year. When integrating over the number of military items types for the given activity (and then over the number of events in a year), these calculations are repeated (accounting for differences in dimensions and numbers) for all military items types used, to obtain the type-specific impact footprint area (I). These impact footprint areas are summed over all military items types for the given activity, and then summed (integrated) over all events to obtain the total impact footprint area resulting from all events occurring in the training or testing area in a given year.

Though marine mammals and sea turtles are not randomly distributed in the environment, a random point calculation was chosen given the available information on an animal's or military item's spatial occurrence. Military items may be expended generally throughout the Study Area, depending on the activity and item type.

The analysis is expected to provide an overestimation of the probability of a strike for the following reasons: (1) it calculates the probability of a single military item (of all the items expended over the course of the year) hitting a single animal at its species' highest seasonal density, (2) it does not take into account the possibility that an animal may avoid military activities, (3) it does not take into account the possibility that an animal may not be at the water surface, (4) it does not take into account that most projectiles fired during training and testing activities are fired at targets, and so only a very small portion of those projectiles that miss the target would hit the water with their maximum velocity and force, and (5) it does not quantitatively take into account the Navy avoiding animals that are sighted through the implementation of mitigation measures (for consideration of mitigation during analysis see Sections 3.4, Marine Mammals; and 3.5, Sea Turtles).

The likelihood of an impact is calculated as the probability (P) that the animal footprint (A) and the impact footprint (I) will intersect within the training or testing area (R). This is calculated as the area ratio A/R or I/R, respectively. Note that A (referring to an **individual** animal footprint) and I (referring to the impact footprint resulting from the **total** number of military items  $N_{mun}$ ) are the relevant quantities used in the following calculations of single-animal impact probability [P], which is then multiplied by the number of animals to obtain the number of exposures (T). The probability that the random point in the training or testing area is within both types of footprints (i.e., A and I) depends on the degree of overlap of A and I. The probability that I overlaps A is calculated by adding a buffer distance around A based on one-half of the impact area (i.e.,  $0.5*I$ ), such that an impact (center) occurring anywhere within the combined (overlapping) area would impact the animal. Thus, if  $L_i$  and  $W_i$  are the length and width of the impact footprint such that  $L_i*W_i = 0.5*I$  and  $W_i/L_i = L_a/W_a$  (i.e., similar geometry between the animal footprint and impact footprint), and if  $L_a$  and  $W_a$  are the length and width (breadth) of the individual animal such that  $L_a*W_a = A$  (= individual animal footprint area), then, assuming a purely static, rectangular scenario (Scenario 1), the total area  $A_{tot} = (L_a + 2*L_i)*(W_a + 2*W_i)$ , and the buffer area  $A_{buffer} = A_{tot} - L_a*W_a$ .

Four scenarios were examined with respect to defining and setting up the overlapping combined areas of A and I:

1. **Scenario 1:** Purely static, rectangular scenario. Impact is assumed to be static (i.e., direct impact effects only; non-dynamic; no explosions or scattering of military items after the initial impact). Hence the impact footprint area (I) is assumed to be rectangular and given by the product of military items length and width (multiplied by the number of military items).  
 $A_{tot} = (L_a + 2*L_i)*(W_a + 2*W_i)$  and  $A_{buffer} = A_{tot} - L_a*W_a$ .
2. **Scenario 2:** Dynamic scenario with end-on collision, in which the length of the impact footprint ( $L_i$ ) is enhanced by  $R_n = 5$  military items lengths to reflect forward momentum.  
 $A_{tot} = (L_a + (1 + R_n)*L_i)*(W_a + 2*W_i)$  and  $A_{buffer} = A_{tot} - L_a*W_a$ .
3. **Scenario 3:** Dynamic scenario with broadside collision, in which the width of the impact footprint ( $W_i$ ) is enhanced by  $R_n = 5$  military items lengths to reflect forward momentum.  
 $A_{tot} = (L_a + 2*W_i)*(W_a + (1 + R_n)*L_i)$  and  $A_{buffer} = A_{tot} - L_a*W_a$ .
4. **Scenario 4:** Purely static, radial scenario, in which the rectangular animal and impact footprints are replaced with circular footprints while conserving area. Define the radius ( $R_a$ ) of the circular

individual animal footprint such that  $\pi * R_a^2 = L_a * W_a$ , and define the radius ( $R_i$ ) of the circular impact footprint such that  $\pi * R_i^2 = 0.5 * L_i * W_i = 0.5 * I$ . Then  $A_{tot} = \pi * (R_a + R_i)^2$  and  $A_{buffer} = A_{tot} - \pi * R_a^2$  (where  $\pi = 3.1415927$ ).

Static impacts (Scenarios 1 and 4) assume no additional aerial coverage effects of scattered military items beyond the initial impact. For dynamic impacts (Scenarios 2 and 3), the distance of any scattered military items must be considered by increasing the length (Scenario 2) or width (Scenario 3), depending on orientation (broadside versus end-on collision), of the impact footprint to account for the forward horizontal momentum of the falling object. Forward momentum typically accounts for five object lengths, resulting in a corresponding increase in impact area. Significantly different values may result from the static and dynamic orientation. Both of these types of collision conditions can be calculated each with 50 percent likelihood (i.e., equal weighting between Scenarios 2 and 3, to average these potentially different values).

Impact probability  $P$  is the probability of impacting one animal with the given number, type, and dimensions of all military items used in training or testing activities occurring in the area per year, and is given by the ratio of total area ( $A_{tot}$ ) to training or testing area ( $R$ ):  $P = A_{tot}/R$ . Number of exposures is  $T = N * P = N * A_{tot}/R$ , where  $N$  = number of animals in the training or testing area per year (given as the product of the animal density [ $D$ ] and range size [ $R$ ]). Thus,  $N = D * R$  and hence  $T = N * P = N * A_{tot}/R = D * A_{tot}$ . Using this procedure,  $P$  and  $T$  were calculated for each of the four scenarios, for Endangered Species Act (ESA)-listed marine mammals and the marine mammal and sea turtle species with the highest average seasonal density (used as the annual density value) and for each military item type. The scenario-specific  $P$  and  $T$  values were averaged over the four scenarios (using equal weighting) to obtain a single scenario-averaged annual estimate of  $P$  and  $T$ . The potential number of exposures ( $t$ ) are reported in Table J-1 through Table J-4.

### J.1.1 PARAMETERS FOR ANALYSIS

Impact probabilities ( $P$ ) and number of exposures ( $T$ ) were estimated for the following parameters:

1. **Two action alternatives:** Alternative 1 and Alternative 2. Animal densities, animal dimensions, and military item dimensions are the same for the two action alternatives.
2. **The following types of non-explosive munitions or other items:**
  - **Small-caliber projectiles:** up to and including .50 caliber rounds
  - **Medium-caliber projectiles:** larger than .50 caliber rounds but smaller than 57 millimeters (mm) projectiles
  - **Large-caliber projectiles:** includes projectiles greater than or equal to a 57 mm projectile
  - **Missiles:** includes rockets and jet-propelled munitions
  - **Bombs:** Non-explosive practice bombs and mine shapes, ranging from 10 to 2,000 pounds
  - **Torpedoes:** includes all lightweight torpedoes
  - **Sonobuoys:** includes all sonobuoys
  - **Targets:** includes expended, airborne and surface, targets, as well as mine shapes
  - **Lightweight torpedo accessories:** includes all accessories that are dropped along with the torpedo (nose cap, air stabilizer, etc.)
  - **Anchors:** includes blocks used to anchor mine shapes to the seafloor
  - **Acoustic countermeasures:** includes aircraft and ship-deployed acoustic countermeasures

- **High-Energy Lasers:** includes high-energy laser weapons that are directed at a surface target
  - **Expeded Bathythermographs:** small sensor deployed from ships or aircraft
3. **Animal species of interest:** The five species of ESA-listed marine mammals and the non-ESA listed marine mammal species with the highest average month density (panropical spotted dolphin). The sea turtle species with the highest average month density in the training and testing areas of interest (green sea turtles).

### J.1.2 INPUT DATA

Input data for the direct strike analysis include animal species likely to be in the area and military items proposed for use under each of the two action alternatives. Animal species data include (1) species identification and status (i.e., threatened, endangered, or neither), (2) highest average seasonal density estimate for the species of interest, and (3) adult animal dimensions (length and width) for the species with the highest density. The animal's dimensions are used to calculate individual animal footprint areas ( $A = \text{length} \times \text{width}$ ), and animal densities are used to calculate the number of exposures (T) from the impact probability (P):  $T = N \times P$ . Military items data include (1) military items category (e.g., projectile, bomb, rocket, target), (2) military items dimensions (length and width), and (3) total number of military items used annually.

Military items input data, specifically the quantity (e.g., numbers of bombs and rockets), are different in magnitude between the two action alternatives. All animal species input data, the military items' identification and category, and the military items' dimensions are the same for the two alternatives; only the quantities (i.e., total number of military items) are different.

### J.1.3 OUTPUT DATA

Estimates of impact probability (P) and number of exposures (T) for a given species of interest were made with the maximum annual number of military items used for each of the two action alternatives. The calculations derived P and T from the highest annual number of military items used in the Study Area for the given alternative. Differences in P and T between the alternatives arise from different numbers of events (and therefore military items) for the two alternatives.

Results for marine mammals and sea turtles are presented in Tables J-1 through J-4.



**Table J-1: Estimated Representative Marine Mammal Exposures from Direct Strike of a High-Energy Laser by Area and Alternative in a Single Year**

Mariana Islands Range Complex		
	Alternative 1	Alternative 2
Humpback	0.000000	0.000000
Sei whale	0.000000	0.000000
Fin whale	0.000000	0.000000
Blue whale	0.000000	0.000000
Sperm whale	0.000001	0.000001
Pantropical Spotted Dolphin	0.000001	0.000001

**Table J-2: Estimated Representative Sea Turtle Exposures from Direct Strike of a High-Energy Laser by Area and Alternative in a Single Year**

Mariana Islands Range Complex		
	Alternative 1	Alternative 2
Green Sea Turtle	0.000025	0.000027

**Table J-3: Estimated Representative Marine Mammal Exposures from Direct Strike of Military Expended Materials by Area and Alternative in a Single Year**

Mariana Islands Range Complex		
	Alternative 1	Alternative 2
Humpback	0.000024	0.000028
Sei whale	0.000008	0.000009
Fin whale	0.000002	0.000002
Blue whale	0.000001	0.000002
Sperm whale	0.000030	0.000035
Pantropical spotted Dolphin	0.000560	0.000660

**Table J-4: Estimated Representative Sea Turtle Exposures from Direct Strike of Military Expended Materials by Area and Alternative in a Single Year**

Mariana Islands Range Complex		
	Alternative 1	Alternative 2
Green Sea Turtle	0.002620	0.003087

## **REFERENCES**

U.S. Department of the Navy. (2017). *Quantifying Acoustic Impacts on Marine Mammals and Sea Turtles: Methods and Analytical Approach for Phase III Training and Testing* (Technical Report prepared by Space and Naval Warfare Systems Center Pacific). San Diego, CA: Naval Undersea Warfare Center.